

Methods for Estimating Intercensal (2000 to 2010) and Postcensal (2010 to 2020) Residential Population by Census Tract

Introduction to Intercensal Estimates, 2000 to 2010

Intercensal estimates of residential population by age (0, 1-4, 5-9, 10-14, 15-19, 20-24, 25-29, 30-34, 35-39, 40-44, 45-49, 50-54, 55-59, 60-64, 65-69, 70-74, 74-79, 80-84, and 85 and over), bridged race (White Non-Hispanic, Black Non-Hispanic, American Indian and Alaska Native Non-Hispanic, Asian and Pacific Islander Non-Hispanic, and Hispanic of any race) and gender were made for all U.S. census tracts for the years 2000 (July 1) to 2010.

Intercensal Estimates, 2000 to 2010, Data Sources and Methods

The residential population estimates for all U.S. census tracts for the years 2000 to 2010 were made by assuming that the proportion of population by age, race, and gender for each tract in a particular county would change linearly from the 2000 and 2010 Census proportions. If a tract had 10% of the county male White Non-Hispanic population age 20-24 in 2000 and 12% in 2010 then for each year 2001 to 2009 the proportion would be a linear interpolation of the 2000 and 2010 proportions. The county total residential population by age, race and gender control estimates for the years 2000 to 2010 were from the NCI SEER Population Estimates database, Vintage 2019.

Census tract data for April 1 2010 are from Census 2010 PCT12H-O tables. The 2010 PCT12 data were summed to the 19 age cohorts and from the single year of age data. Asian Alone Non-Hispanic (PCT12L) and Native Hawaiian and Other Pacific Islander Alone Non-Hispanic (PCT12M) were summed to create Asian and Pacific Islander Alone Non-Hispanic. Other Non-Hispanic (PCT12N) and Two or More Races Non-Hispanic (PCT12O) population by age and gender were distributed proportionally to the four race groups based on the county proportion of Some Other Race Non-Hispanic and Two or More Races Non-Hispanic by race, gender and age for 2010.

The census tract definitions for all years, 2000 to 2010 are the 2010 Census census tract definitions. The 73,057 census tracts in the United States based on 2010 census tract definitions. The 2000 Census data in 2010 census tracts were estimated from the IPUMS data for 2000 Census Tables P5 and P12A-I. To estimate the 2000 data in 19 age cohorts, by gender, and by five race groups the P12 table age cohorts were summed to the 19 age cohorts. Asian Alone (P12D) and Native Hawaiian and Other Pacific Islander Alone Non-Hispanic (P12E) were summed to create Asian and Pacific Islander Alone. Black or African American Alone Non-Hispanic, American Indian and Alaska Native Alone Non-Hispanic, Some Other Race Non-Hispanic and Two or More Races Non-Hispanic were estimated by subtracting Hispanic (P12H) less the difference of White Alone (P12A) less White Alone Non-Hispanic (P12I) and then distributing Hispanic not White by age, gender, and race using a constant proportion of total Hispanic Population by Race (P5) for each census tract. The age and gender estimates obtained using the total Hispanic by race population proportions were constrained to both the total Hispanic not White for each gender and age cohort and to P5 data.

Other Non-Hispanic and Two or More Races Non-Hispanic population by age and gender were distributed proportionally to the four race groups based on the county proportion of Some Other Race Non-Hispanic and Two or More Races Non-Hispanic by race, gender and age for 2000.

Intercensal Estimates, 2000 to 2010, Data Sources and Methods (continued)

The proportions of each race, gender, age cohort for 2000 and 2010 were made by dividing each census tract by the sum of all tracts in a particular county. These proportions were interpolated for 2001 to 2009 (as described above) and multiplied by county July 1 population for 2000 to 2010 to obtain census tract population by age, gender, and race for all years, 2000 to 2010.

Two sets of estimates were prepared for 2000 to 2010 (based on 2010 geographies) to reflect county and parish adjustments for hurricanes Katrina and Rita.

Introduction to Postcensal Estimates, 2010 to 2020

Postcensal estimates of residential population by age (0, 1-4, 5-9, 10-14, 15-19, 20-24, 25-29, 30-34, 35-39, 40-44, 45-49, 50-54, 55-59, 60-64, 65-69, 70-74, 74-79, 80-84, and 85 and over), bridged race (White Non-Hispanic, Black Non-Hispanic, American Indian and Alaska Native Non-Hispanic, Asian and Pacific Islander Non-Hispanic, and Hispanic of any race) and gender were made for all U.S. census tracts for the years 2010 (July 1) to 2020. The residential population estimates for all U.S. census tracts for the years 2010 to 2020 were made using a hybrid regression, demographic, and proportional model.

Postcensal Estimates Census Tract Data for 2000 and 2010

Census tract data for April 1, 2010 were from Census 2010 PCT12H-O tables. The 2010 PCT12 data were summed to the 19 age cohorts from the single year of age data. Asian Alone Non-Hispanic (PCT12L) and Native Hawaiian and Other Pacific Islander Alone Non-Hispanic (PCT12M) were summed to create Asian and Pacific Islander Alone Non-Hispanic. Other Non-Hispanic (PCT12N) and Two or More Races Non-Hispanic (PCT12O) population by age and gender were distributed proportionally to the four race groups based on the county proportion of Some Other Race Non-Hispanic and Two or More Races Non-Hispanic by age, race, and gender for 2010.

Census tract data for April 1, 2000 were estimated from IPUMS data for 2000 Census Tables P5 and P12A-I. To estimate the 2000 data in 19 age cohorts, by five race groups, and by gender the P12 table age cohorts were summed to the 19 age cohorts. Asian Alone (P12D) and Native Hawaiian and Other Pacific Islander Alone Non-Hispanic (P12E) were summed to create Asian and Pacific Islander Alone. Black or African American Alone Non-Hispanic, American Indian and Alaska Native Alone Non-Hispanic, Some Other Race Non-Hispanic and Two or More Races Non-Hispanic were estimated by subtracting Hispanic (P12H) less the difference of White Alone (P12A) less White Alone Non-Hispanic (P12I) and then distributing Hispanic not White by age, race, and gender using a constant proportion of total Hispanic Population by Race (P5) for each census tract. The age and gender estimates obtained using the total Hispanic by race population proportions were constrained to both the total Hispanic not White for each gender and age cohort and to P5 data. Other Non-Hispanic and Two or More Races Non-Hispanic population by age and gender were distributed proportionally to the four race groups based on the county proportion of Some Other Race Non-Hispanic and Two or More Races Non-Hispanic by age, race, and gender for 2000.

Postcensal Estimates Proportional Model for Census Tracts

An estimate was made of total population by age and gender and of population by age, race, and gender of all years 2010-2020 for all census tracts. These proportional estimates were by age and gender (38 cohorts) were used to control the results of the demographic model to specific age gender cohorts. A second set of proportional model estimates were also made for census tract population by age, race, and gender (190 cohorts). The 190 cohort proportional estimates by age, race, and gender were used to evaluate the demographic model results.

The proportional model assumes that the 2010 proportion of a county (C) age, gender, race cohort for a particular census tract (CT) remain constant for all years 2011 through 2020. For example, for any year t, 2011 through 2020, White male population age 20-24 were estimated as:

$$WM-CT_{20-24}_t = (WM-CT_{20-24}_{2010} / WM-C_{20-24}_{2010}) \times WM-C_{20-24}_t$$

Total population for a census tract in the 190 cohort proportional model is not a constant proportion of the county for the year 2011 to 2020 because the age, race, and gender cohorts of the tract change at different rates based on Vintage 2020 county population changes by age, race, and gender for the years 2011 to 2020.

The proportional model results for all census tracts in a particular county for each age, race, and gender cohort exactly sum to the county totals without any constraining algorithms because the sum of the proportions always equal one.

Postcensal Estimates Regression Model for Census Tracts

For census tracts that were expected, based on contemporaneous data or observations, to grow significantly more rapidly, or more slowly, than the county total, then a lagged ordinary least squares (OLS) regression model was used to allow for divergent growth of particular census tracts.

Census tract total population was split into two age cohorts: 0-39 and age 40+. American Community Survey (ACS) 5-year census tract (based on 2010 geographies) total population age 0-39 and 40+ data for the years 2010 to 2019 were used to identify potential census tracts for the regression model.

The functional forms of all census tract (CT) OLS equations were:

$$TPOP-CT_{0-39}_t = f(TPOP-CT_{0-39}_{t-1})$$

$$TPOP-CT_{40+}_t = f(TPOP-CT_{40+}_{t-1})$$

The coefficients for each of the two age cohorts were applied identically to all age, race, and gender cohorts within the two OLS cohorts.

The OLS results were not constrained to county totals or to proportional model total population by age and gender census tract totals.

Postcensal Estimates Regression Model for Census Tracts (continued)

If the following conditions were met for a particular census tract, then the regression model was used to estimate population by age, race, and gender for that census tract:

1. the ACS population year to year change for both cohorts must be either all positive or all negative in at least eight of the nine years, 2010-2011 through 2018-2019;
2. all years of the ACS population data, 2010 to 2019, must be greater than zero for both cohorts, i.e. 0-39 and 40+;
3. if a coefficient was greater than 1.0 it must also be greater than the county population average annual rate of growth, 2010 to 2019; similarly, if a coefficient was less than 1.0 it must also be less than the county population average annual rate of growth, 2010 to 2019;
4. adjusted R-squared for both equations must be greater than 0.80.

In total, 833 regression models were used (1,666 equations;) 17 of the regression models had coefficients less than 1.0 and 816 had coefficients greater than 1.0. The average adjusted R-squared was 0.902 and the average T-statistic of the coefficients was 62.4.

Postcensal Estimates Demographic Model for Census Tracts

Estimates were made for each of the 190 age, race, and gender cohorts for each census tract for the year 2020 with census tract data for 2000 and 2010 using a modified Hamilton-Perry method [1,2] with imposed constraints and exogenous boundaries.

Implicit survival rates and fertility rates were calculated for each of the 190 age, race, and gender cohorts for each census tract based on 2000 and 2010 data for each tract. The implicit survival and fertility rates were then used to estimate 2020 census tract population by age, race, and gender.

For the 15 age cohorts 10-14 through 80-84 by race and gender an implicit survival rate was used to estimate 2020 census tract population. For example, 2020 White male population age 20-24 for a particular census tract was estimated as:

$$WM_{20-24}_{2020} = (WM_{20-24}_{2010} / WM_{10-14}_{2000}) \times WM_{10-14}_{2010}$$

This was repeated for all 15 age cohorts by 5 race groups by gender.

The age cohort 85+ by race by gender was estimated using a similar implicit survival rate. For example, 2020 White male population age 85+ for a particular census tract was estimated as:

$$WM_{85+}_{2020} = (WM_{85+}_{2010} / WM_{75+}_{2000}) \times WM_{75+}_{2010}$$

This was repeated for 85+ population by 5 race groups by gender.

Postcensal Estimates Demographic Model for Census Tracts (continued)

The age cohorts 0, 1-4, and 5-9 were estimated using implicit fertility rates by race. For example, 2020 White male population ages 0, 1-4, and 5-9 for a particular census tract were estimated as:

$$WM_0_{2020} = (WM_0_{2010} / WF_{15-44}_{2010}) \times WF_{15-44}_{2020}$$

$$WM_{1-4}_{2020} = (WM_{1-4}_{2010} / WF_{15-44}_{2010}) \times WF_{15-44}_{2020}$$

$$WM_{5-9}_{2020} = (WM_{5-9}_{2010} / WF_{20-49}_{2010}) \times WF_{20-49}_{2020}$$

The population by age, race, and gender for 2011 to 2019 were estimated by linearly interpolating 2010 and 2020 estimates for each of the 190 age, race, and gender groups for each census tract.

In some cases the initial results of the demographic model, prior to constraining, yielded dramatic population changes for specific census tracts. Approximately 5.2% of all census tract age, race, and gender implicit survival rate estimates for 2020 were either greater than 8.0 or less than 0.5 and were adjusted to these limits. However, even with these limits imposed some census tracts had total population results greater than 1.7 times or less than 0.7 times total population results from the proportional model. If the demographic model exceeded these bounds (greater than 1.7 times or less than 0.7 times total population results from the proportional model) for a particular census tract, then the 190 cohort proportional model was used for that census tract. A total of 5,292 census tracts used the 190 cohort proportional model in place of the demographic model because the demographic model yielded results that were out of bounds.

Constraining Postcensal Estimates to County Totals

An iterative bi-directional constraining, or raking, algorithm was used to constrain, or control, the census tract estimates to county totals. The results of both the demographic model and the 190 cohort proportional model (which was used in place of demographic model results for some census tracts), were constrained to both the county total for the cohort and to the census tract total population by age and gender cohort determined in the 38 cohort proportional model for total population by age and gender. The county total to which the 190 cohorts were constrained was the difference of county population less any census tract regression model estimates so that the regression model estimates were not constrained to county totals; similarly, regression model estimates were not constrained to the 38 cohort proportional model results for a particular tract.

References

- [1] Hamilton, C.H., and Perry, J., 1962, "A Short Method for Projecting Population by Age from One Decennial Census to Another", *Social Forces*, vol. 41, pgs. 163-170.
- [2] Swanson, D.A., 2010, "Forecasting the Population of Census Tracts by Age and Sex: An Example of the Hamilton-Perry Method in Action", *Population Research and Policy Review*, vol. 29, pgs. 47-63.

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